

# New Nonlinear Analyses Methodology: Displacement Capacity of Piles

Presented at  
Prevention First 2010 – Long Beach, CA

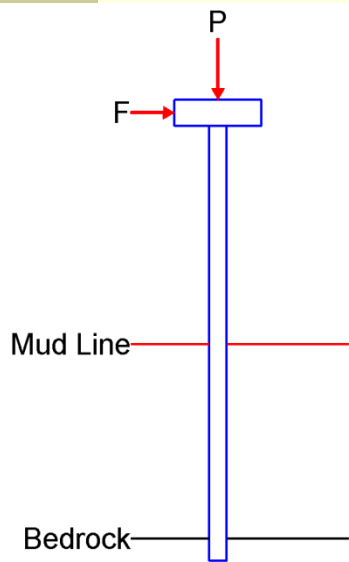
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# Objectives

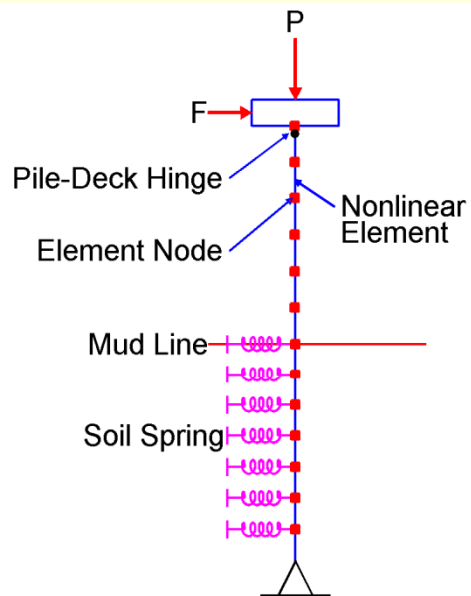
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- Develop a simple model to estimate displacement capacity of piles in Marine Oil and LNG Terminals
  - Satisfy strain MOTEMS material strain limits
  - Eliminate need for pile nonlinear pushover analysis
- Evaluate “accuracy” of simple model

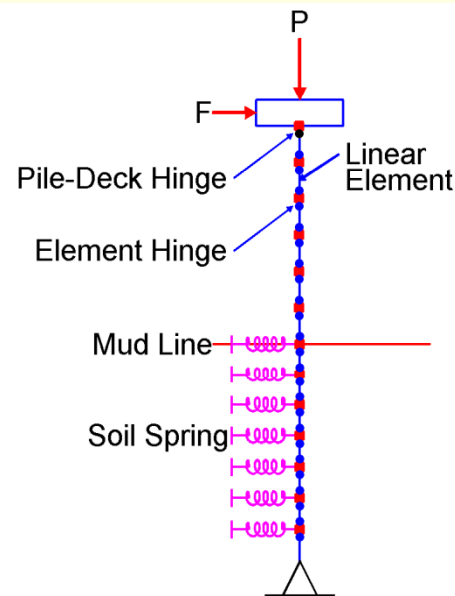
# Pile Model for Seismic Analysis



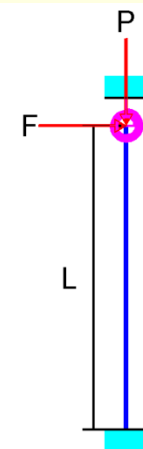
Pile-Deck System



Model with Nonlinear Elements

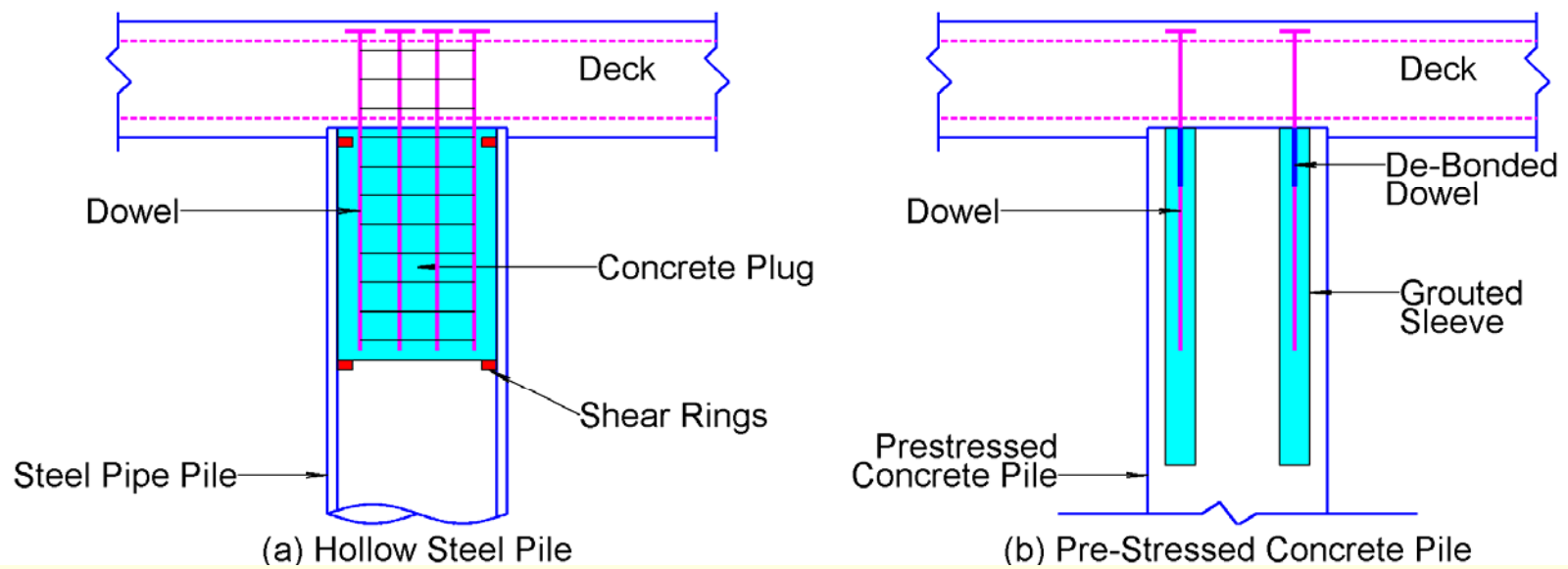


Model with Linear Elements and Hinges



Simple Model

# Piles-Deck Connection



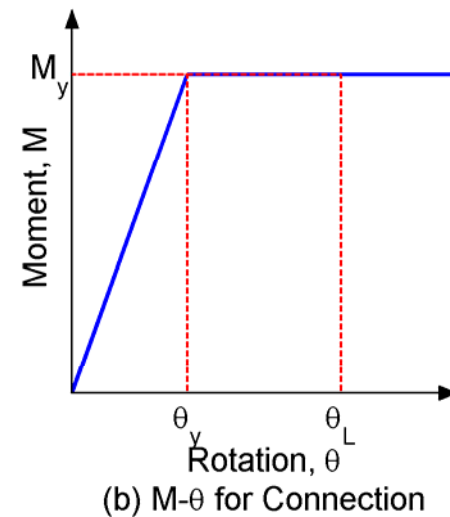
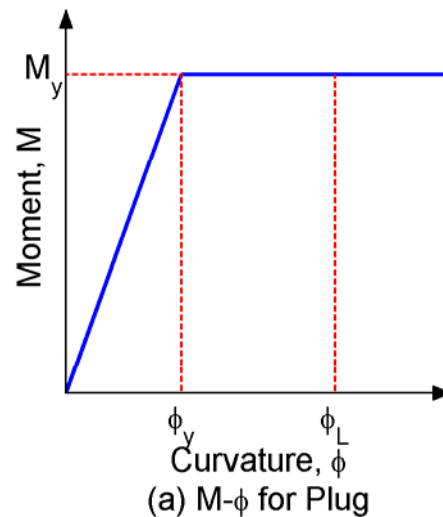
# Pile-Deck M-θ Relationship

$$\theta_y = L_{sp} \phi_y$$

$$L_{sp} = 0.12 f_{ye} d_{bl}$$

$$\theta_L = \theta_y + \theta_P$$

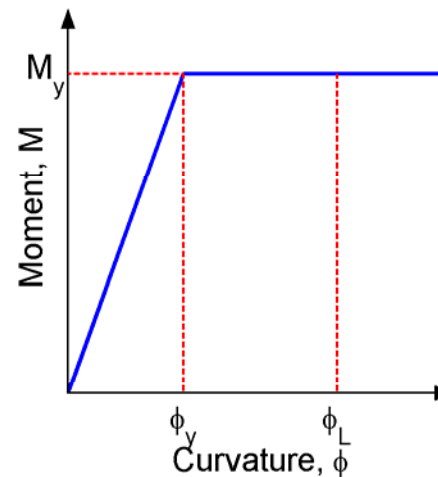
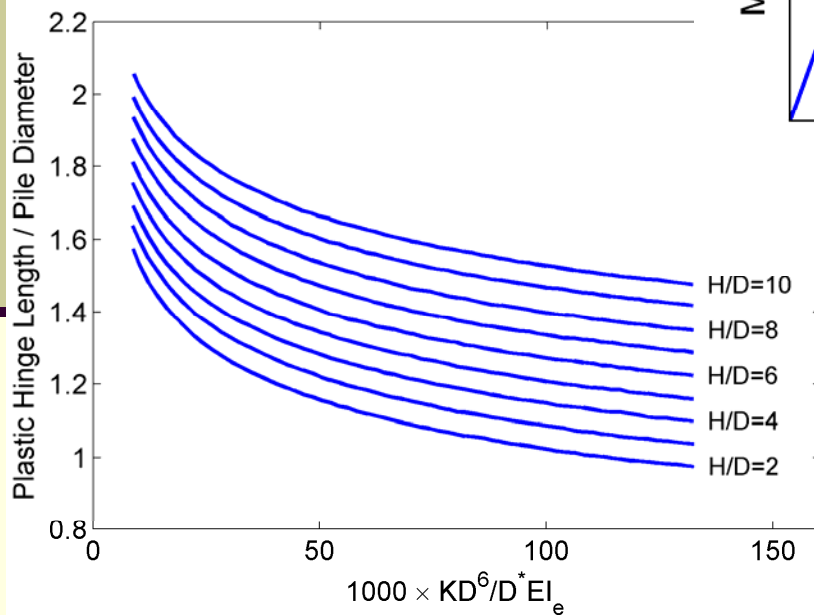
$$\theta_P = L_P (\phi_L - \phi_y)$$



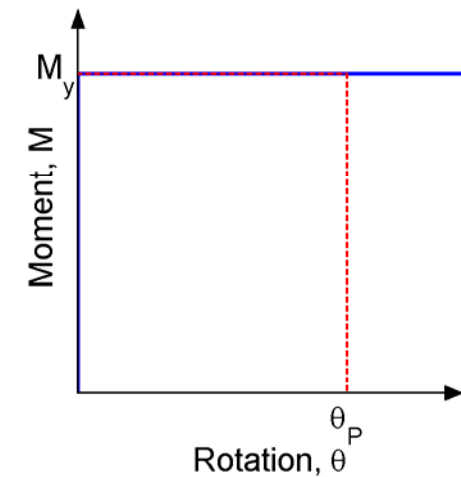
$$L_P = \begin{cases} 0.08L_e + 0.12f_{ye} d_{bl} \geq 0.2f_{ye} d_{bl} & \text{for PS Concrete} \\ 0.3f_{ye} d_{bl} + d_{gap} & \text{for Hollow-Steel} \end{cases}$$

# In-Ground Pile Hinge M- $\theta$ Relationship

$$\theta_P = L_P (\phi_L - \phi_Y)$$

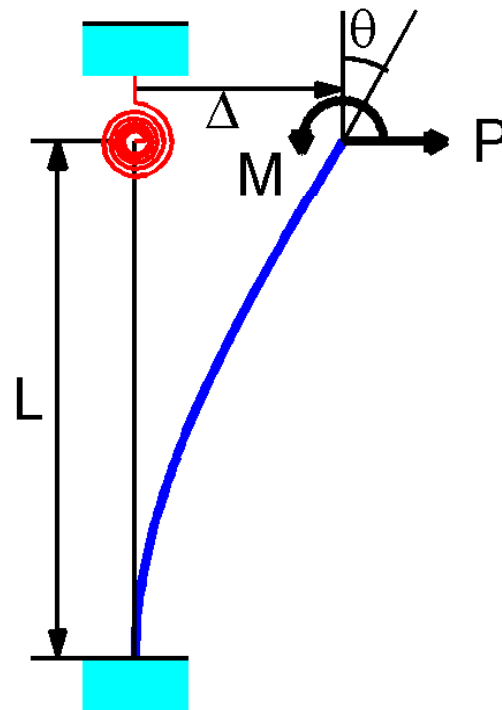


(a) M- $\phi$  for Pile Section

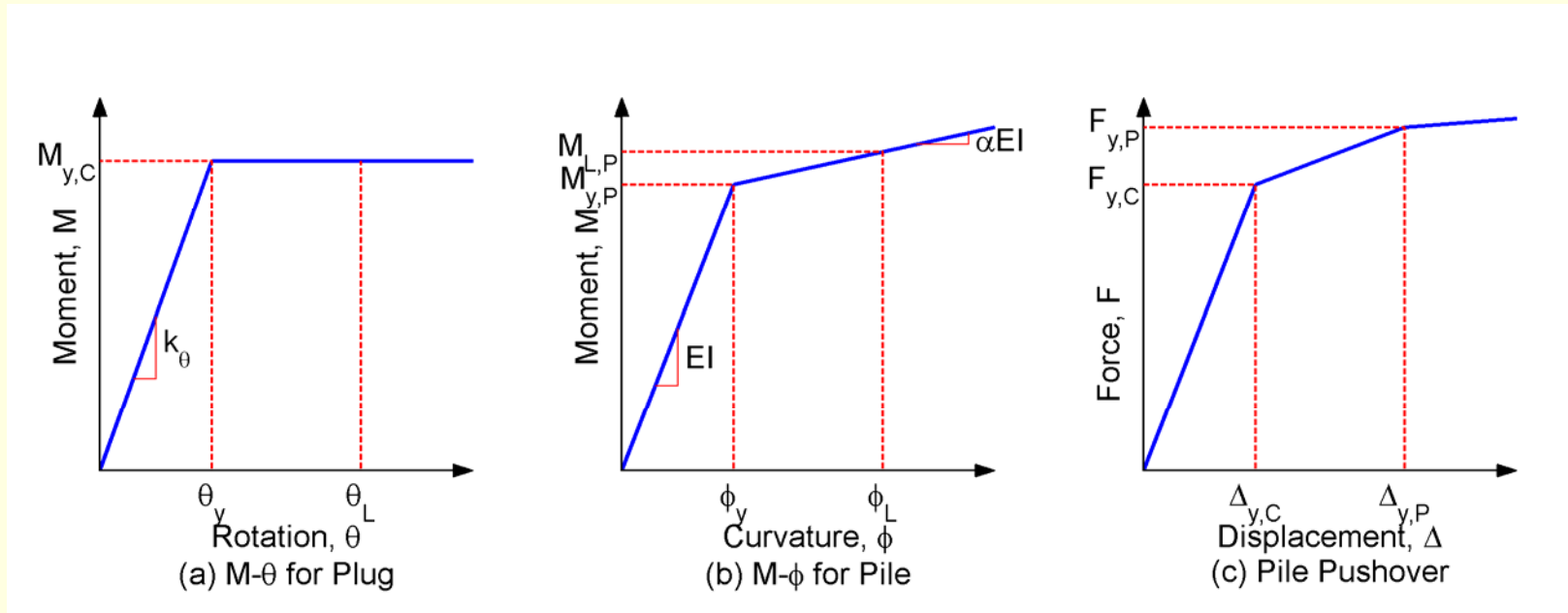


(b) M- $\theta$  for Pile Hinge

# Simplified Model



# Simplified Model



Idealized behavior assumed in development of formulas for ductility capacity of piles with plug-connection to the deck



# Ductility Capacity: Connection Hinging

$$\mu_{\Delta,C} = \begin{cases} \frac{1 + 4\beta\mu_{\theta}}{1 + 4\beta} & \text{for } \mu_{\theta} \leq \frac{\eta - 1}{2\beta} \\ \frac{2 - \eta + 6\beta\mu_{\theta}}{1 + 4\beta} & \text{for } \mu_{\theta} > \frac{\eta - 1}{2\beta} \end{cases} \quad \eta = \frac{M_{y,P}}{M_{y,C}}$$
$$\beta = \frac{EI}{k_{\theta}L}$$

$\mu_{\theta}$  = Rotation ductility of plug at selected design

$k_{\theta}$  = Moment-Rotation stiffness of plug

$EI$  = Effective  $EI$  of pile

$L$  = Pile length of equivalent displacement-fixity

# Ductility Capacity: Pile Hinging

$$\mu_{\Delta,P} = \frac{2\eta - 1}{1 + 4\beta} + \left( \frac{6\eta}{1 + 4\beta} \right) \left( \frac{\rho\eta}{1 + \eta} \right) \left( 1 - \frac{\rho\eta}{2(1 + \eta)} \right) (\mu_{\phi} - 1) \quad \eta = \frac{M_{y,P}}{M_{y,C}}$$
$$\beta = \frac{EI}{k_{\theta}L}$$

$\mu_{\phi}$  = Curvature ductility of pile at selected design

$k_{\theta}$  = Moment-Rotation stiffness of plug

$EI$  = Effective  $EI$  of pile

$L$  = Pile length of equivalent displacement-fixity

$\rho$  = Plastic hinge length as a fraction of pile length

# Displacement Capacity

$$\Delta_{y,c} = \frac{\theta_{y,c} L (1 + 4\beta)}{6\beta}$$

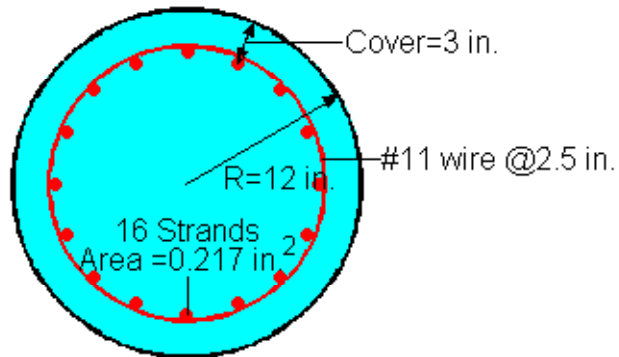
$$\eta = \frac{M_{y,P}}{M_{y,C}}$$

$$\beta = \frac{EI}{k_{\theta} L}$$

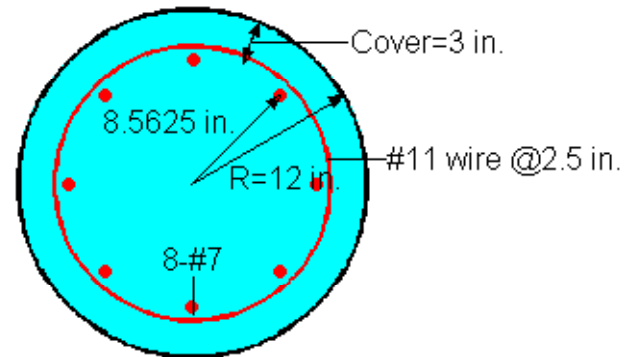
$\theta_{y,c}$  = Yield rotation of plug/dowel connection

$$\Delta = \Delta_{y,c} \times \{ \mu_{\Delta,C}, \text{ or } \mu_{\Delta,P} \}$$

# Pre-Stressed Concrete Pile

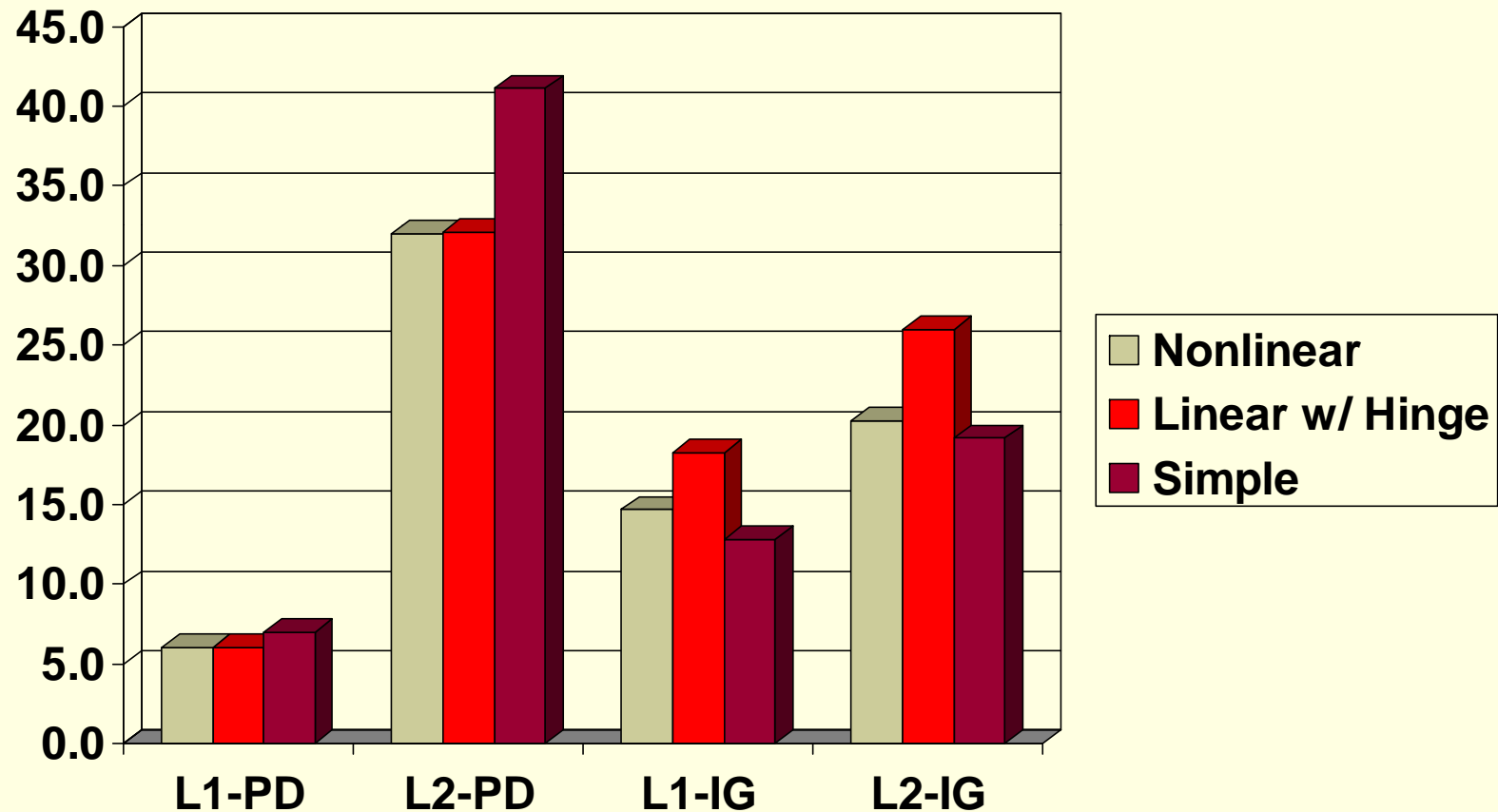


(a) Pile Section

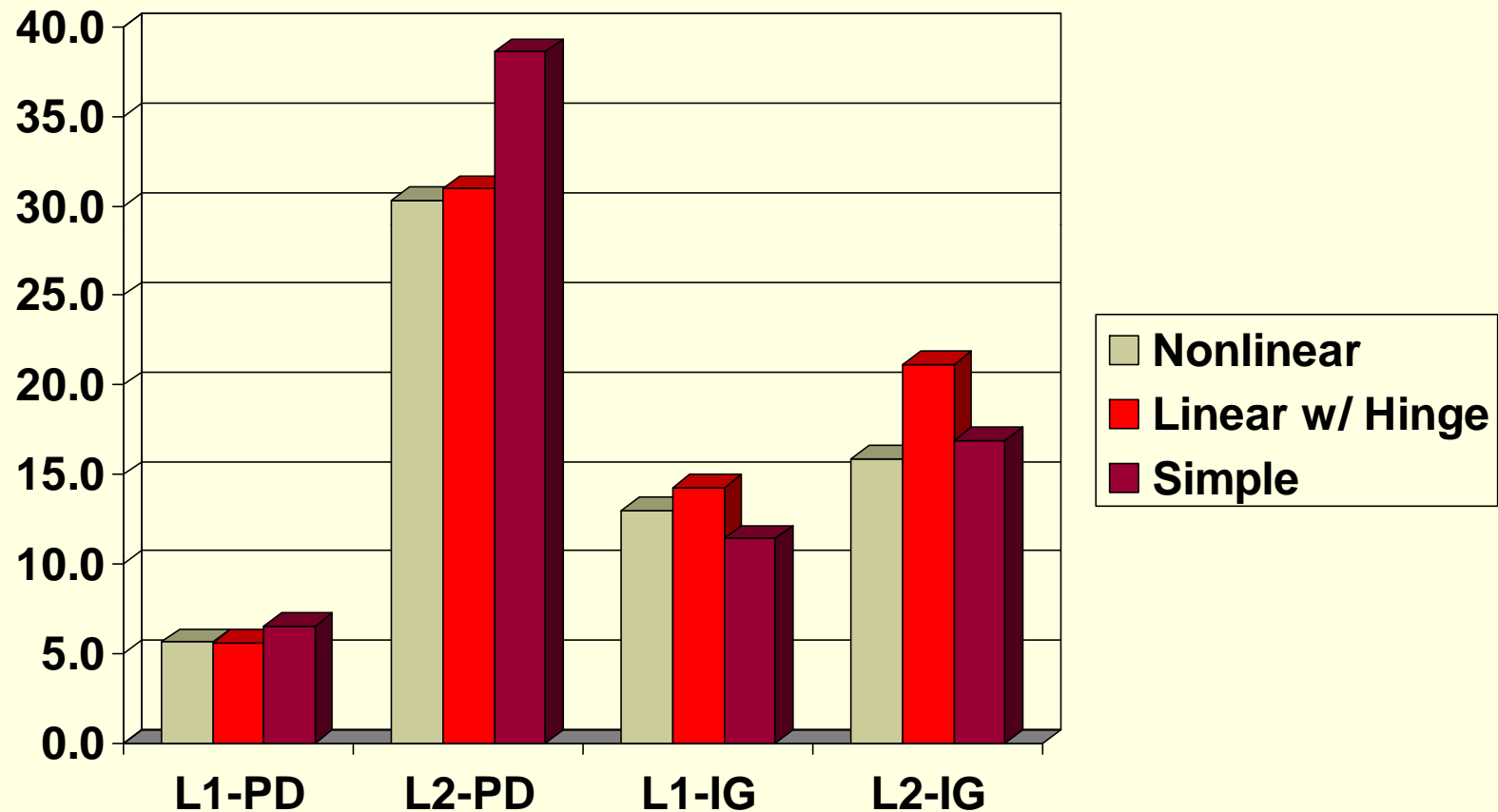


(b) Dowel Connection

# Displacement Capacity: $K = 0.2$ kip/in<sup>3</sup> (Medium Clay)



# Displacement Capacity: $K = 0.5$ kip/in<sup>3</sup> (Stiff Clay)



# Conclusions

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- Simple model provides results “accurate” enough for practical purposes
  - Use for preliminary design
  - Check on results from detailed nonlinear pushover analysis

# Conclusions

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- Model with linear beam and plastic hinges provides reasonable results
  - Requires assumption on plastic hinge length
  - Limited data for current in-ground plastic hinge length recommendations in MOTEMS
  - Displacement capacity appears to very sensitive to plastic hinge length assumption



# Recommendations

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- Develop in-ground plastic hinge length charts for piles typically used in Marine and LNG Terminals considering appropriate soil conditions
  - Current recommendations are based on Cast-In-Drilled-Hole (CIDH) piles for bridges
- Develop moment-rotation model for pile-deck connections
  - Traditional models based on plastic hinge length may not be applicable